

PHY 117 HS2023

Week 12, Lecture 1

Dec. 5th, 2023

Prof. Ben Kilminster

Last time, standing waves:
in general

$$y(x,t) = 2A \cos \omega t \sin kx$$

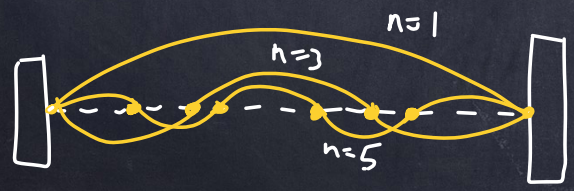
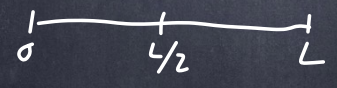
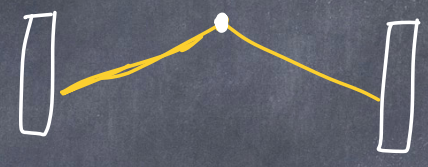
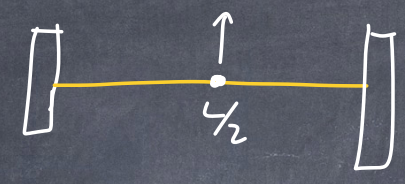
where $k_n = \frac{n\pi}{L}$ + $\omega_n = k_n v$ + $v = \frac{\omega}{k}$
 $\omega_n = 2\pi n f_1$

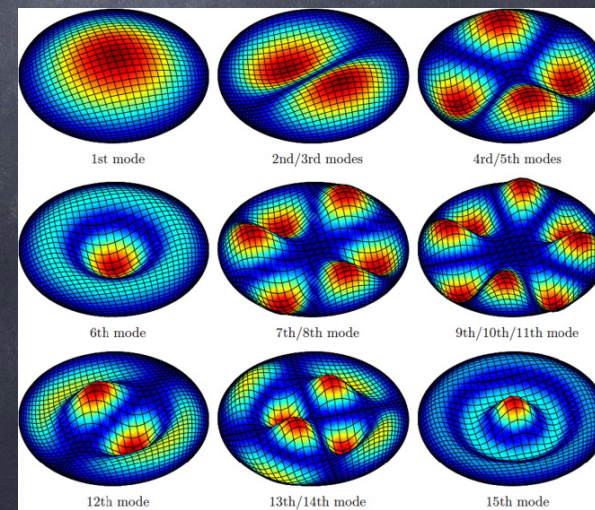
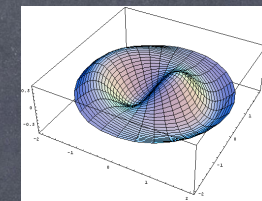
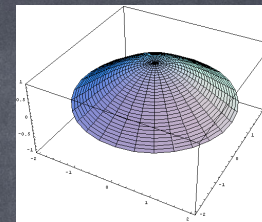
$$f_1 = \frac{v}{\lambda_1} = \frac{k_1 v}{2\pi}$$

Example:
standing
wave
on string

$n=4$  $k_4 = \frac{4\pi}{L}$, $\omega_4 = k_4 v$, $v = \sqrt{\frac{T}{\mu}}$










Wavelengths for Different States

For a hydrogen atom:

Electron wave resonance
 $n = 1$

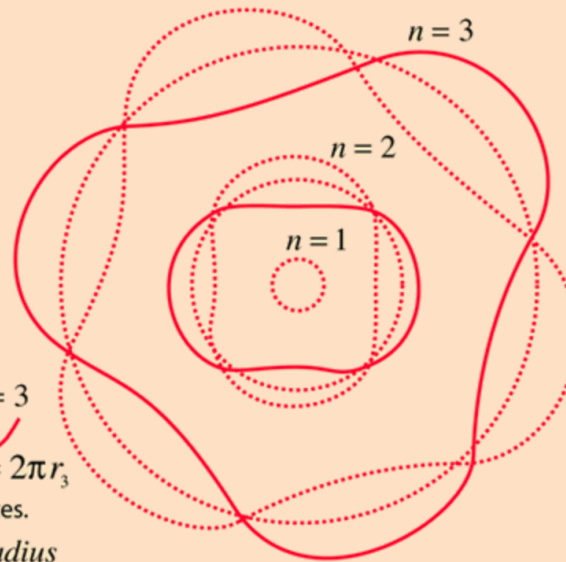
 $\lambda_1 = 2\pi r_1 = 6.28a_0$

 $n = 2$
 $2\lambda_2 = 2\pi r_2$
 $\lambda_2 = 12.57a_0$

 $n = 3$
 $\lambda_3 = 18.85a_0$ $3\lambda_3 = 2\pi r_3$

Wavelengths for hydrogen states.

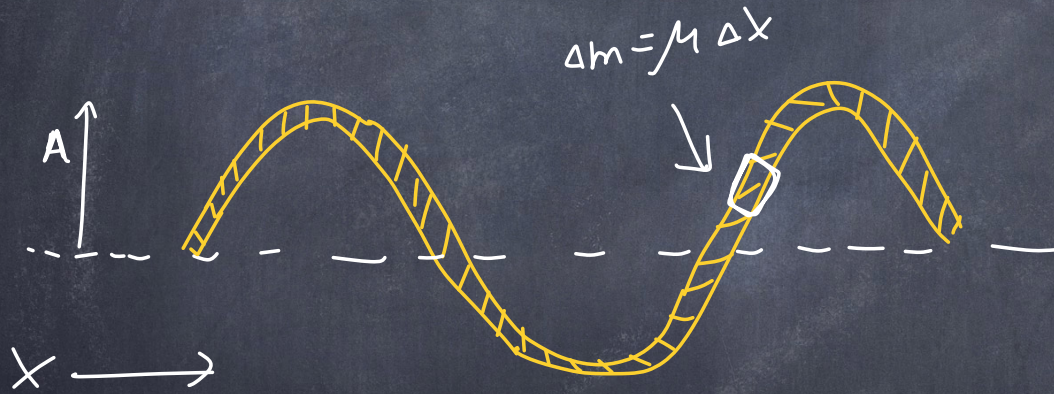
$a_0 = 0.0529\text{nm} = \text{Bohr radius}$



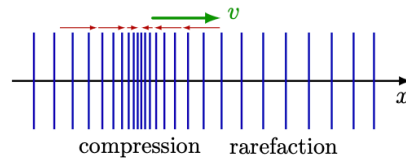
[Index](#)

[Bohr
model
concepts](#)

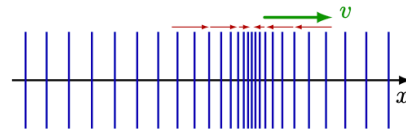
[Bohr model of the atom](#)





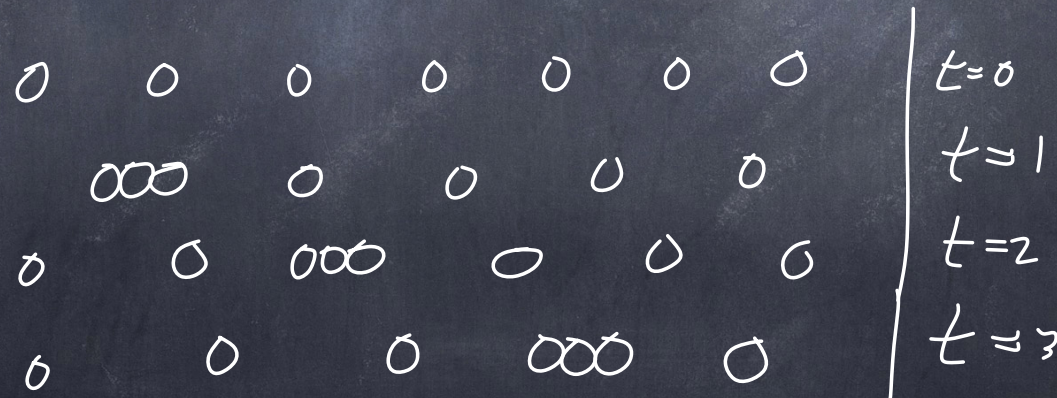


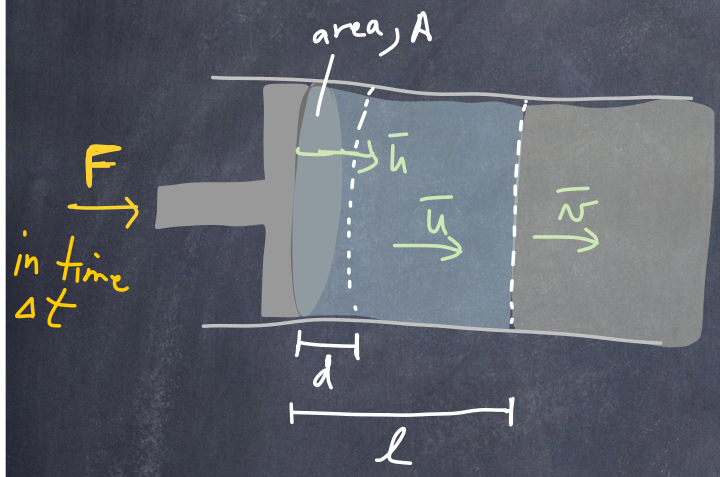
(a) Time $t = 0$.



(b) Time $t = \Delta t$.

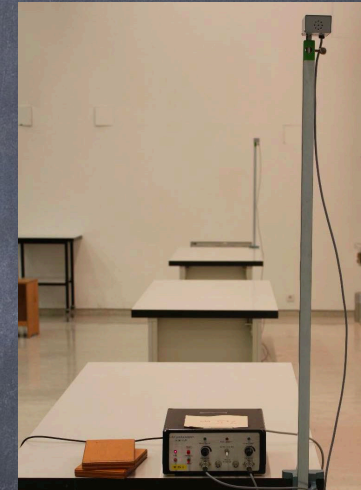
Figure 13.10: A traveling longitudinal wave is when the distortion happens along the direction of propagation, here shown as a local displacement.

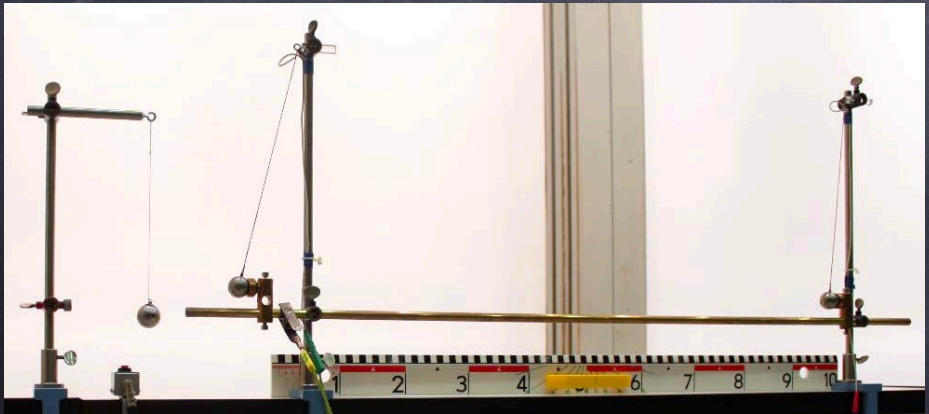


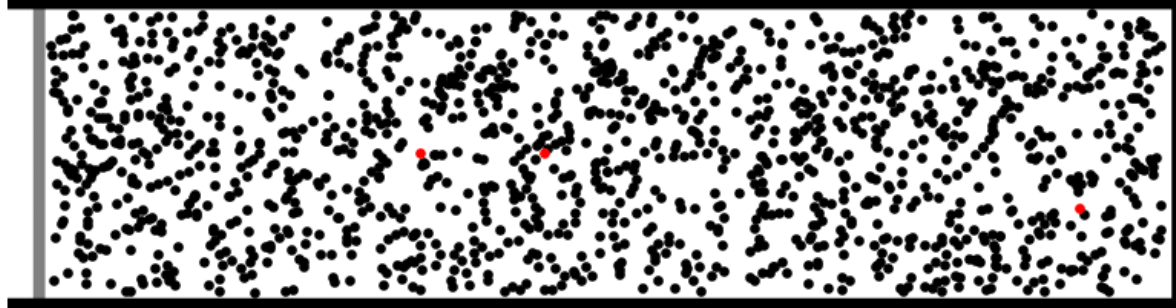




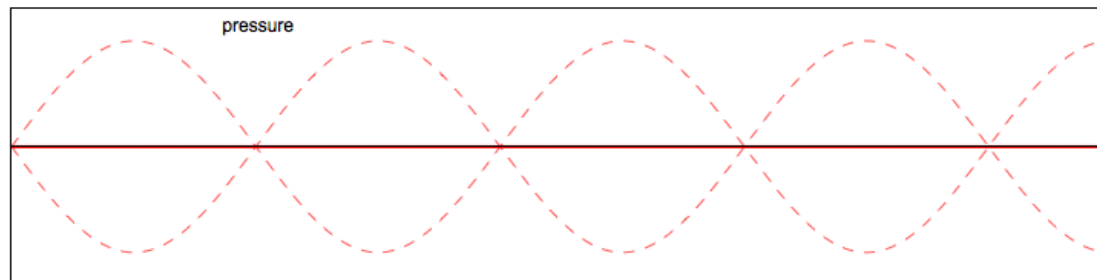
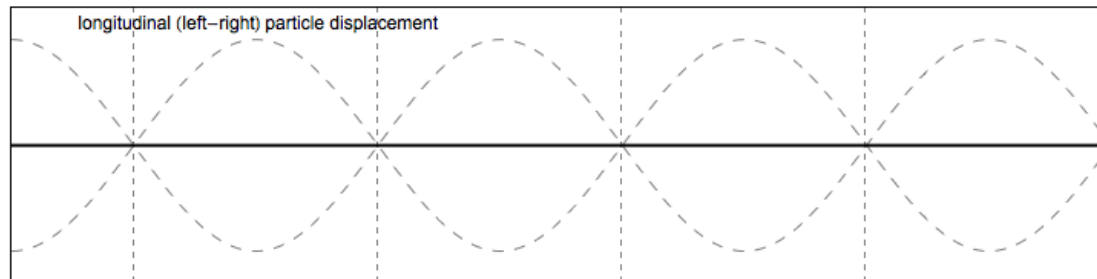


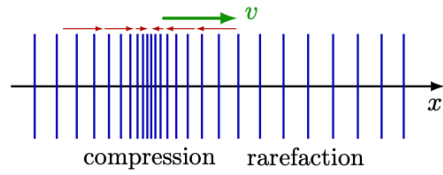




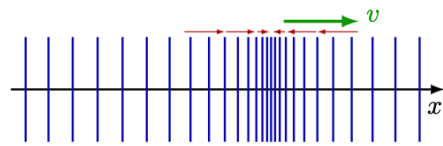


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(a) Time $t = 0$.



(b) Time $t = \Delta t$.

Figure 13.10: A traveling longitudinal wave is when the distortion happens along the direction of propagation, here shown as a local displacement.

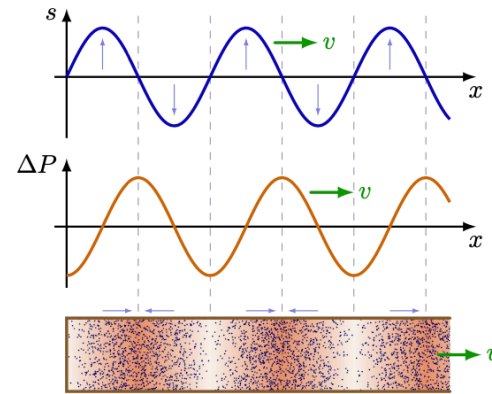
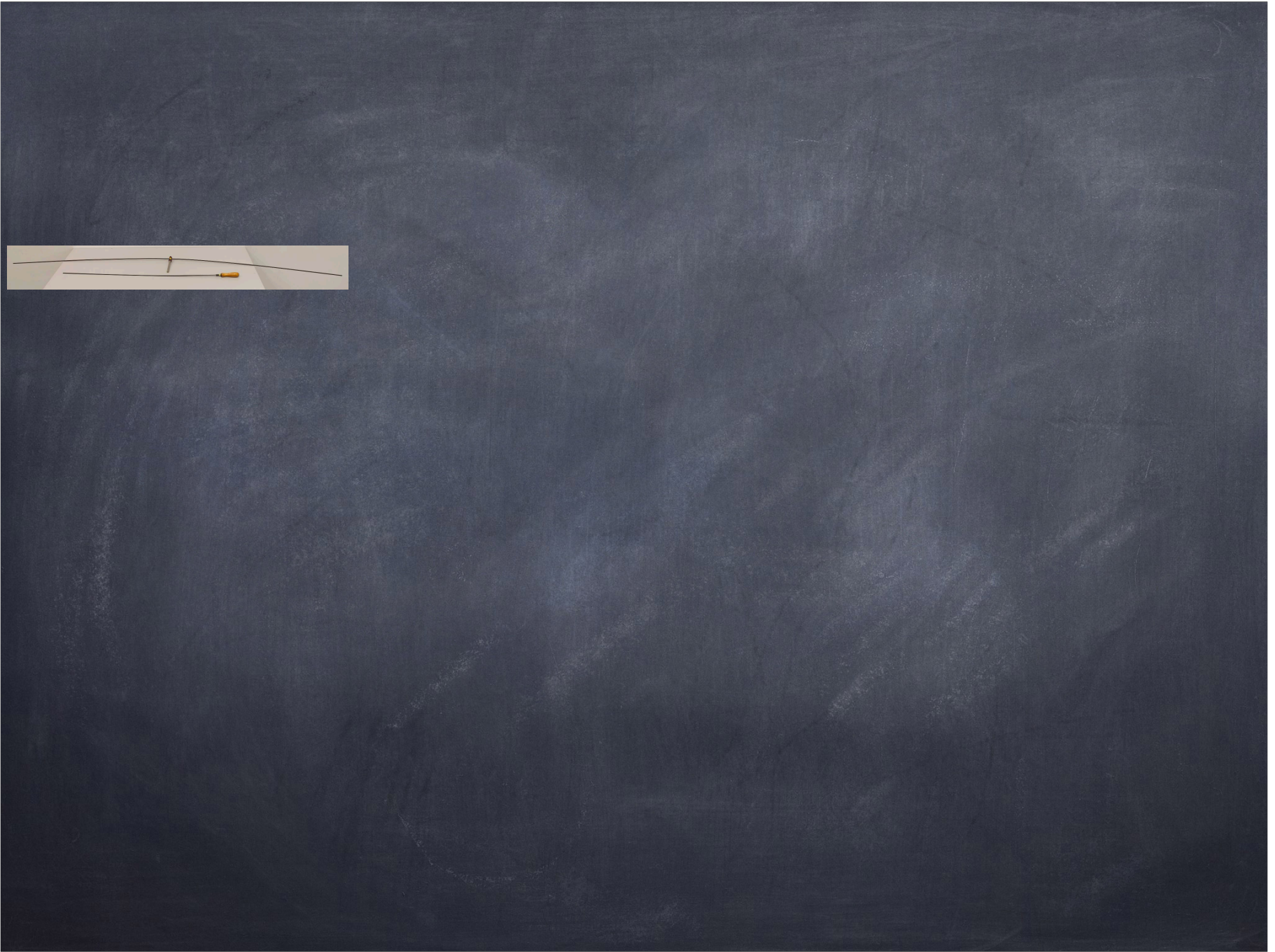
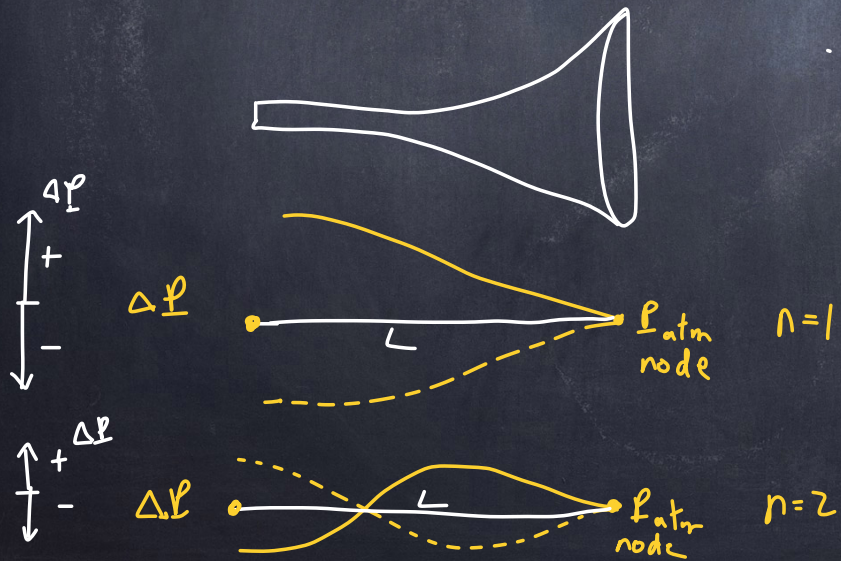


Figure 13.11: Sound wave traveling in a tube of air, shown as a local, average displacement s of air molecules in the longitudinal (x) direction (blue), and a local pressure variation ΔP (orange), 90° out of phase with s .

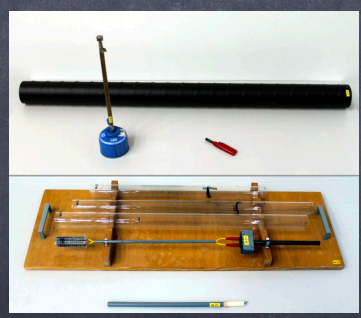
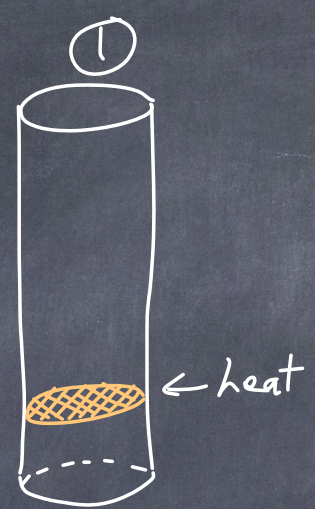


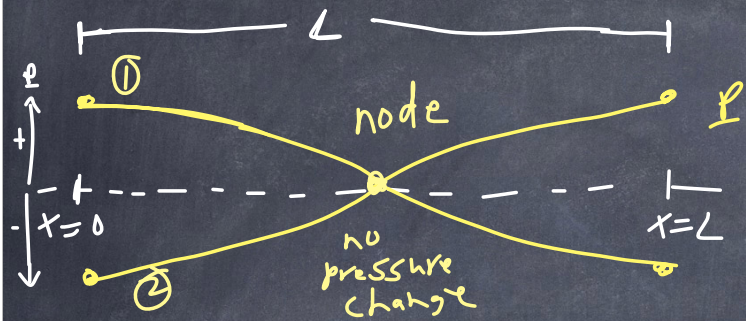


Alphorn

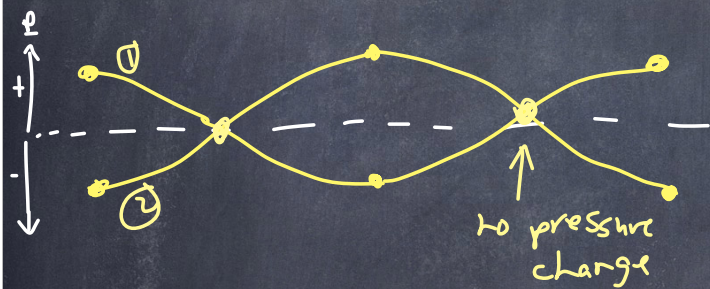




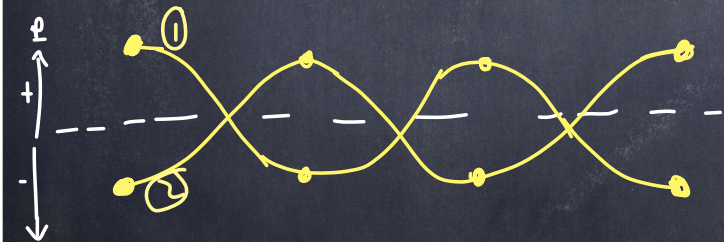




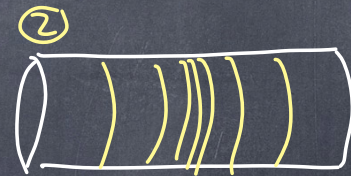
$n=1$



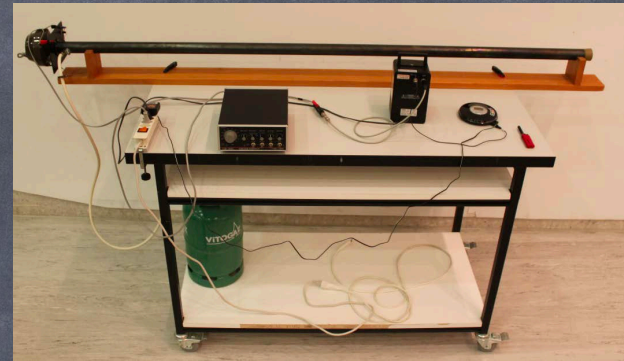
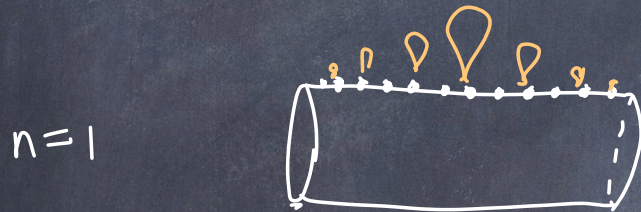
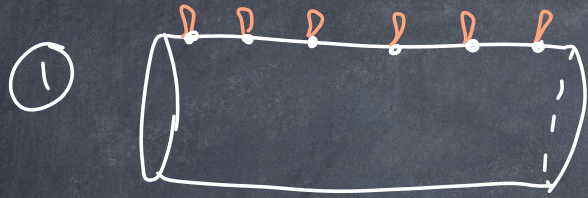
$n=2$

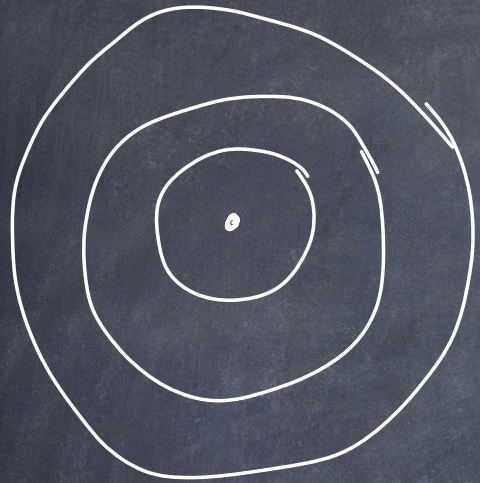


$n=3$



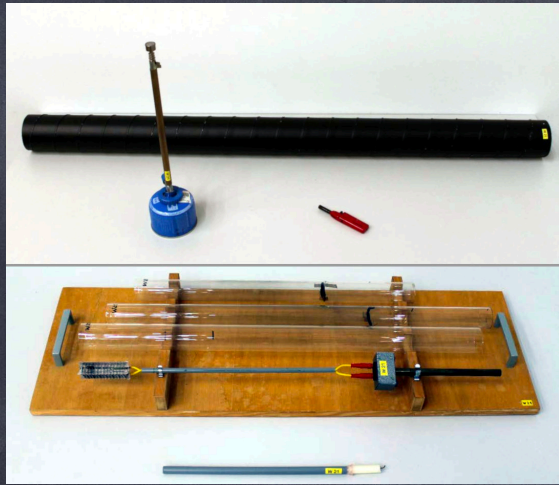
Ruben's flame tube







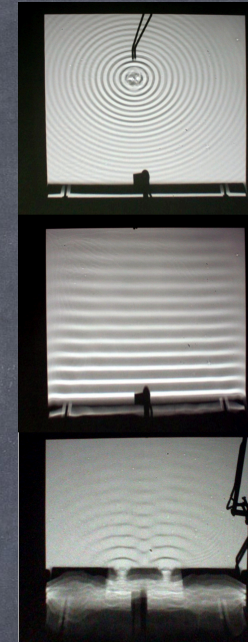




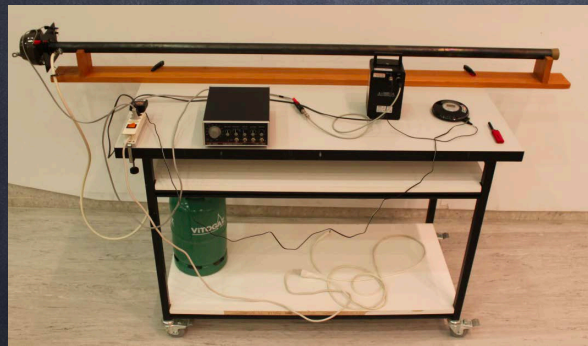
W21



W13



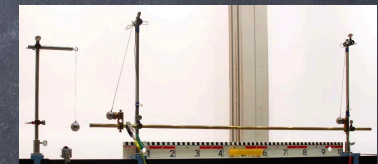
W108



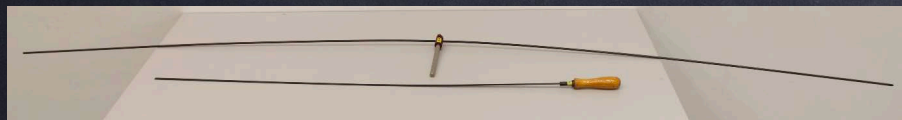
W34



W110



W32



W36

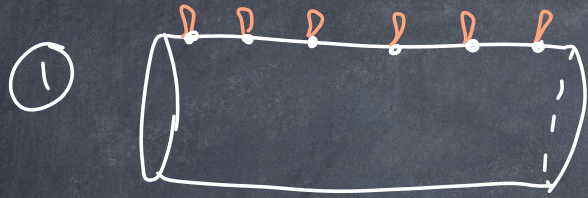


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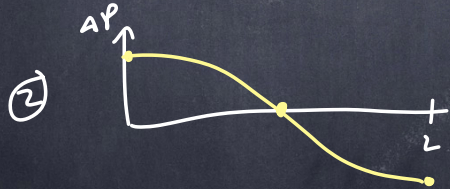
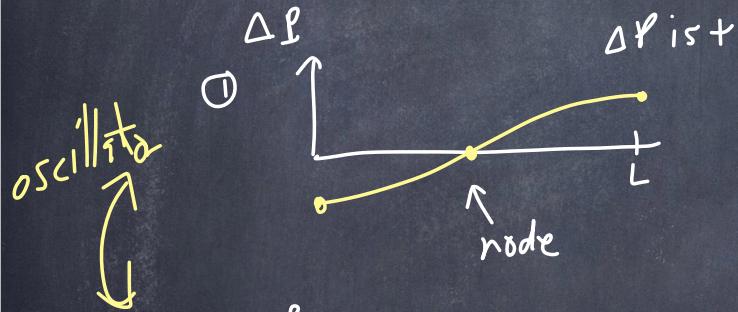


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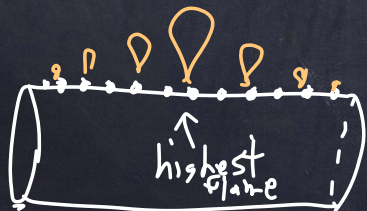
Ruben's flame tube



$n=1$

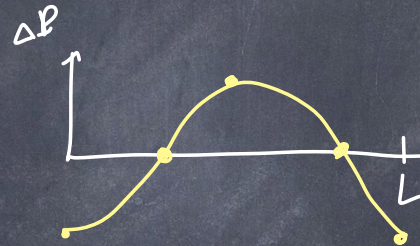
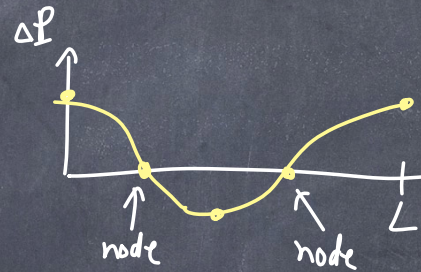


① → ② → ① ...



flame is higher
at node because
 ΔP is smaller than
 P_{atm}
(see next page)

$n=2$



For quiet sounds, ΔP of the gas $<$ P of the gas

From Bernoulli's equation, gas flow is proportional to square root of the pressure difference between inside + outside tube.

$$\text{Flow} \sim \sqrt{P_{\text{inside}} - P_{\text{outside}}}$$

(The flow of gas out of the pipe)

$\Delta P_{\text{maximal}}$, anti-nodes produce lower flames
(flow rate is lower)

$\Delta P = 0$, nodes, flow rate is higher

Part of the cycle, pressure is higher than average
but part is lower. On average

This is why pressure is higher at nodes:

$$\sqrt{\text{Pressure difference at anti-nodes}} < \sqrt{\text{Pressure at nodes}}$$